Algorithms - Network

A NON-PLANAR, LANE-BASED NAVIGABLE DATA MODEL

FOR ITS

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approach has been generally useful and widely accepted, it is only one of many possible paradigms. In an effort to increase the number and improve the quality of network applications, research has been undertaken to develop and employ a fully non-planar representations is also discussed. routing across lanes is presented. The relative efficiency of planar and non-planar provide a test of the utility of the new model, thus a discussion of the challenges posed by utilizing new types of feature connectivity. Houte finding functions will ultimately be used to previously unattainable level of network detail. These enhancements involve identifying and representation. Further, the use of lanes as the primary geographic element has provided a Digital network databases traditionally employ a fully-intersected planar data model. While this

Key words

Non-planar, data modeling, ITS, lanes, networks.

1. Introduction

or processes that will be modeled and the variable functionality of the Based on the designers' knowledge of the pertinent transportation functions vary in its ability to serve the needs of any given transportation function. limit the functionality of the database. Each unique feature representation will definition, the development of such a data model requires a comprehensive distinct representations, and enables the user to manipulate the phenomena disciplines, a digital geographic data model is generally defined as an available data models, the appropriate representation can be chosen. which the user intends to apply. Decisions regarding the model components knowledge of both the phenomena to be represented and the manipulations when held in the system as data (Raper and Maguire, 1992). Given this While the concept of the data model is used in a variety of ways by numerous information structure which allows the user to store specific phenomena as

the following topics related to network data modeling: modeling documented in the NCGIA Final Report (1994). This paper covers Highway Systems (ITS). This research is an extension of the planar data The primary purpose of this paper is to clearly outline the research and development of a non-planar, lane-based data model for Intelligent Vehicle

- A review of planar data models;
- Variability in planar restrictions;
- A comparison of storage requirements for planar and non-planar features;
- The impact of data resolution on the data model design;
- The development of a non-planar, lane based data model;
- The application of network functions to the model.

Planar data models

of the line segments (including transportation segments). The widespread paradigm into their spatial analytic tools (ESRI 1991a). ARC/INFO and other software systems which have incorporated this acceptance and use of the fully intersected model, has been reinforced by households are located is satisfied by a fully intersected planar data model to associate census data with these polygonal areas within which individual included to allow the census geographic regions to be well defined. The need geographic regions for which data is collected. Therefore, they must be transportation features are often coincident with boundaries of the census correct and maintain the database while they use it. More importantly, the enumerators in locating "fugitive" households. The also allows enumerators to (TIGER/LineO Files 1992). The transportation network has been included in TIGER for a number of reasons. First, the roads are provided to assist I his allows the creation of polygons based on the left and right side attributes industry leading Geographic Information System (GIS) software developers Line Graph (DLG) series of products from the United States Geologic Survey Bureau of the Census (and their precursors the DIME files), and the Digital widely used, national map databases - in particular, the Topologically The most commonly used data model for transportation networks is the fully intersected, planar data model. This is an artifact of the prevalence of several (USGS) - and the acceptance of the fully intersected model by a number of Integrated Geographic Encoding and Referencing (TIGER) files from the

new features or intersections are added. The need to split current features at amount of attribute error into such databases. This is expecially true when these numerous features has been responsible for introducing a substantial continuous feature. The labor intensive process of entering and maintaining could be described as an uninterrupted range of values for the single have identical attributes along their lengths, or they have attributes which which in reality represent a single continuous feature. Often the segments maintenance of the feature attributes for a large number of street segments, the end point of each segment. This in turn requires the input and proliferation of transportation line segments due to the fully intersected data and for some applications unacceptable. Of greatest concern is the intersected data models place on transportation planning are considerable, beneficial to the transportation community. However, the limitations that fullythe fully intersected data model demands an intersection with a node marking model. At any intersection of linear features - whether physical or statistical -The presence of a consistent national transportation database is extremely

that time demands that attributes, such as address ranges, be updated appropriately. This is not an insignificant problem. Moreover, the need to access a large number of segments for any single continuous feature adds to the selection and computation time of transportation functions over the network. The error among the feature attributes is transferred to the network functions applied over the network; these functions can only reasonably be expected to perform as accurately as the attribute data on which they rely. While the obvious positional inaccuracies of several early databases have been a continuous irritant to many users, these errors are primarily a function of the technology used for data capture rather than an artifact of the data model (Spear 1991).

These liabilities have given rise to the current interest in non-planar transportation network models. It is expected that the development of a non-planar prototype will improve on the fully intersected data model in its utility for transportation related applications. While the exploration of this type of data model has been stifled by the inertia of the previously mentioned data collection sources and analytic tools (which have a vested interest in the fully intersected planar model), this also allows for substantial freedom in the decisions made here regarding the development of the prototype.

3. Variability in planar restrictions

Non-planar networks are broadly defined as those networks which allow segments of the network to cross without a network node being located at the intersection. There is, in fact, no implicit or explicit contact between the line segments at the point of intersection. This conceptual model is common in traditional graph theory, and is, in fact, necessary when considering transport modes without well defined, physical routeways. Shipping lanes, for example, often cross in mid-ocean without any node capable of accepting attributes (beyond the approximate location) occurring at the point of intersection. The same is true for airline networks.

Therefore, a non-planar network commonly consists of links and nodes without the mandatory requirement that every intersection be associated with a node. This allows node attributes to be associated with true network intersections but limits the proliferation of unnecessary line segments and unrealistic node placement. Houting of automobiles across such a network is more accurately implemented due to the elimination of impossible turns at multiple-grade crossings (underpass/overpass). Furthermore, users often consider a fully-intersected database to be a less accurate representation of reality, with some nodes solely being artifacts of the data model.

While some unnecessary line segments are eliminated by allowing non-planar intersections, the vast majority of intersections in an urban transportation network are true planar intersections. This suggests that the traditional definition of a non-planar network allows only a relatively small improvement in database size to be achieved, while the functionality of planar systems for polygonal spatial analysis is wholly lost. This research proposes that, if the

 $x_b = I + \sqrt{I + 2x_p}$

representation. the improvement in database storage acquired by switching to a non-planar parts of many urban areas. The difference between x_b and x_p is a measure of organized in a nxn matrix. This is not unrealistic for some urban areas, or for With this equation one can find x_b given x_p if we assume that the streets are matrix, for an arbitrary n:

External data model - lanes and spatial information

or other driving parameters. Many secondary attributes which are crucial to often have more than one direction of traffic, lanes vary with respect to turn streets as homogenous line features. For example, multiple lane streets very variation of lane attributes within single street features it is clear that many included for display in the prototype data model. However, due to the the continuous street feature. Most importantly, the lanes themselves can begin or end at any point along lanes. Among these are travel time by mode, traffic flow, and congestion. access, lanes can restrict mode use, and lanes can be made to control speed ITS functions are dependent on the inclusion of individual lanes rather than discussed above, the continuous street features will be the smallest element process of selecting real world features for inclusion in the database. As External data modeling as described by Laurini and Thompson (1992) is the ITS applications are based on these physical and mandated attributes of

specific lane. Consequently, using lanes as features for display would mislead for analysis, and uses streets as the primary display feature. dispensing. Therefore, this data model utilizes lanes as the primary element users regarding the accuracy of the data the system was receiving and within 10 meters. This accuracy is not sufficient to locate a vehicle on a locations on the surface of the Earth can only be absolutely known only surface. Based on known sources of error, it is generally accepted that Ideally, lanes would be used as display features as well as primary elements. measurements are made in comparison to a benchmark on the Earth's GPS technology purports to provide up to centimeter accuracy, Unfortunately, several issues of accuracy prohibit lane representation. While

points along the relevant street. with the spatial information for lanes being limited to start points and end individual polylines. Rather, the street should be stored as a single polyline, to GPS accuracy. For these reasons, there is no value in storing lanes as same general path, and the variation from that path is not significant relative internal data structure. All lanes associated with a street or highway follow the The available accuracy also affects how spatial information is stored in the

defined feature to be represented by a single record in the map database segments at any intersection. This allows each physically continuous, wel planar data model described herein will not utilize nodes to separate line with a single feature. benefit from this relaxed constraint should be maximized. Therefore, the nonplanar enforcement is going to be compromised by the data model, the This, in turn, eliminates the repetition of identical attribute data associated This results in a substantially more compact database with far fewer features

Data model feature comparisons

connectivity of the network. Thus the reduction in features through conversion represented through different data models is a function of the size and be less than or equal to x_p - 1. the number of features in a non-planar version of the same network, x_0 , will Thus, if the number of features in a planar network is represented by x_p , then one of the features) the non-planar data model will contain fewer features. features cross (and if they cross at a point that is not an endpoint for at least However, as long as there is a single intersection where two continuous from a planar to a non-planar data model will be unique to each network. The difference in the number of features between identical networks

also totally unrealistic. Commonly transportation networks are well connected, unimpressive, but the assumption of a network with only one intersection is equivalence. non-planar data models based on matrix size, and a statement of their statements of the relationship between numbers of features in planar and reduction in features is a function of the grid or matrix size. Below are two connectivity in rectangular grid networks is consistent within the network, the and in urban centers often take the form of a rectangular grid. Because This minimum possible improvement in feature quantity is dramatically

4.1 Planar vs. non-planar feature numbers for an n x m matrix

North-South streets. The total number of non-planar features is n+m. Consider an nxm matrix of streets to be a set of n East-West streets and m

 x_p = the number of features in a planar model

 x_b = the number of features in a non-planar model

n(m-1) arcs. Similarly there are m(n-1) North-South arcs. Total arcs is thus: South street creating m-1 arcs. For all East-West streets there are therefore In the planar model each East-West street intersects with each m North-

For the case where n=m: n(m-1) + m(n-1) = 2mn-m-n

 $x_p = 2n^2 - 2n$

allows one to determine the number of non-planar arcs, given only the non-planar arcs will grow much more slowly. An algebraic transformation As n increases the number of planar arcs will increase with the square of n, number of planar arcs and the special condition that the network is a nxn

The essential fields of the lane table are given in Table 1. Each lane in the database has a unique record in this table, with a corresponding unique identifier stored in the *lane_id* field. The identifier for the street associated with each lane, that is, the polyline the lane follows, is stored in the *street_id* field. Start and end positions of each lane are stored in the *from* and *to* fields, respectively. These positions are given as linear offsets from the beginning of the street polyline.

FIELD	TYPE	DESCRIPTION
lane_id	integer	Unique lane identifier
street_id	integer	Street identifier
from	real	Start position of lane
to	real	End position of lane

Table 1 Lane table.

This method of storing spatial information for lanes is similar to the way linear attributes are modeled using dynamic segmentation in ARC/INFO. Specifically, a lane represented by reference to a particular street polyline with a start and end point is analogous to a linear event referenced to a particular route with a start and end point (ESRI 1991b). However, in ARC/INFO, the route is the basic element and the linear event is an attribute of that element. In the lane based model, the lane is the basic element, while the street polyline is used to store spatial information. For this reason, lanes must contain additional information not associated with linear events: the relationship between lanes. This relationship takes the form of lane connectivity, making the model an integrated representation of the real world, rather than a simple collection of spatial elements.

Feature interconnectivity

A fundamental part of any transportation network data model is the interconnectivity of the basic data elements. If a model does not store, in some fashion, how the elements are connected there can be no analysis of flow between elements. This also precludes routing across the network, a major part of ITS applications.

In the traditional planar data model, with links as the basic data element, interconnectivity is represented by nodes. Links sharing nodes are connected at those nodes (NCGIA 1994). Typically, however, there is a need for further restriction of the interconnectivity. In a model of a street network, planar enforcement can cause a node to exist where there is no actual intersection. An example of this would be a freeway overpass, where a street passes over a freeway on a bridge. Since the street and the freeway each cross over the same point on the ground, planar enforcement requires a node at that location, even thought there is no actual intersection. A second common example is the case of legal turn restrictions, where there is an actual

intersection, but drivers are not legally allowed to change directions at that intersection. In both of these instances, the data model must restrict the connection between links.

One standard method used to handle this is the inclusion of a turn restriction table in the data model. This table stores, for each node, the turn restrictions for that node. This turn restriction table can also be used to store turn impedances to more realistically model the real world situation. The ARC/INFO data model uses this method for handling turn restrictions. Each node in the network may have entries in the turn table, identifying an incoming link and an outgoing link, along with information about the impedance of that connection. The maximum number of entries in the table for each node is equal to the square of the number of links sharing that node, but an entry is not required for each link pair. Missing entries are interpreted as having zero impedance, so that it is not necessary to explicitly specify zero impedances are used to disallow connection between two links sharing a node (ESRI 1992).

Another approach is required in the non-planar, lane based data model discussed here. Because intersections are not represented by nodes in the model, turn information must be stored differently. The intention of this model is to accurately represent traffic flow in lanes, so it is appropriate to store turn information as a lane attribute. It is not sufficient, however, to simply list turning options at the end of a lane, because it is frequently possible to turn at more than one point along a lane. In addition, the case of parallel lanes requires the model to allow turns along a linear segment of a lane. In this instance, it is possible to switch lanes at any point along the segment. These segments do not have to continue for the entire length of a lane. Legal or physical barriers may prevent lane changes for certain distances. This is commonly seen in the case of car pool lanes, or when a lane is closed due to an accident or construction (NCGIA 1994). Because of these complexities in the lane based model, the model must be able to store turn information at multiple points and along multiple segments.

The requirement of storing multiple turn possibilities for each lane makes it effectively impossible to include turn information in the same table as lanes. In a relational database this information can be stored in a separate table, similar to the turn table in ARC/INFO. The storage method differs, however, in the method of referencing the turns, because of the complexities discussed above. Two types of turns need to be stored: turn availability at a point on a lane, and linear turn availability along a segment of a lane.

Impedance points must also be introduced into the model. These points indicate places where traffic must slow or stop, even if no turn is made. In the planar data model, this is handled implicitly: even when traveling straight through an intersection a "turn" is made, which may have an impedance value. Again, in the non-planar lane based model, there is no node to use to store impedances, so we must use a different method. Similarities between a turn point and an impedance point strongly suggest that impedance points be

6.1 Tums at points

these types will be discussed in order.

stored with the turns, so we will consider that a third type of turn. Each of

While the lane based model is much more complex in terms of connectivity than the planar link-node model, it does have one distinct advantage: lanes only have one direction. In the planar model, movement is possible in both directions along a link, unless it is explicitly prohibited. In the lane based model, movement is only allowed in the fundamental direction of a lane. This implies an extremely straightforward method of storing turn information in a relational database. A table can be used to store a description of each turn possibility in every lane in the database. While this table is likely to be large, proper sorting should make access very efficient.

	-	impodence
End Position on Destination Lane	real	to_position
Turn Destination Lane	integer	to_lane
Start Position on Origin Lane	real	position
Unique Turn Identifier	integer	tum_id
Tum Origin Lane	integer	lane_id
DESCRIPTION	TYPE	FIELD NAME TYPE

Table 2 Point turn table.

Consider the basic point turn table definition shown in Table 2. The six fields shown are the essential elements of a turn table in this model. The first field, lane_id, contains the identifier of the lane. This value references a unique entry in the lane table (Table 1). The second field, turn_id, is the identifier of the turn, unique within each lane. The field pair consisting of lane_id and turn_id is unique in the turn table, and can be used to reference turns globally in the database. The positional information of the turn along the lane is stored in the position item, giving the offset along the street containing the lane at which the turn is located.

The destination point of the turn is given in the next two items. To_lane indicates the destination lane, and references the lane_id item in the lane table. The to_position field specifies the location along the to_lane where the connection occurs. The final item in the table, impedance, contains the impedance value of making that turn. Additional fields can be added to this table containing time-based restrictions or impedances, or other turn attributes. If the table is sorted with lane_id as the primary key and position as the secondary key, the first turn along a lane can be found using a binary search algorithm, then turns can be processed in the order in which they actually occur in the physical network. Disallowing turns in the database can be handled quickly by "turning off" the turn by assigning a negative value to the impedance field.

6.2 Turns along segments

Turns along segments can represented in a fashion similar to point turns, with a table containing one entry per turn. However, differences in the turn types require a few changes in the fields. Rather than a simple turn position, the linear turns require a start position and an end position. In addition, the turn destination depends on where along the segment the turn is made, rather than being a single position on the destination. The turn also not only has an associated impedance, as with point turns, but also a travel distance required to complete the turn. A basic linear turn table definition is shown in Table 3.

Impedance of the turn	real	impedanc
Linear distance required to complete the turn	real	distance
Location on the to_lane corresponding to the start_position of the turn	real	to_offset
Destination lane of the turn	intege	to_lane
Location of the end of the turn on the lane	real	end
Location of the beginning of the turn on the	real	start
Unique turn identifier	intege	tum_id
Lane on which the turn occurs	intege	lane_id
DESCRIPTION	TYPE	FIELD

Table 3 Linear turn table.

Four of the items in this table are identical to items in the point turn table previously discussed (Table 2): $lane_id$, $turn_id$, to_lane and impedance. These items have the same meaning in both tables. The position and $to_position$ fields in the point turn table are missing in this table, with the analogous information stored in other fields. Start and end together represent the location of the turn in the lane, with start giving the beginning location of turn availability and end giving the ending location. This indicates that the turn may be taken at any point along the lane between start and end.

In the point turn table, the destination point is given as a single location (position) along the to_lane. The situation is more complex in the linear turn table. First, the destination point is dependent on the location where the turn is actually taken, not just where the turn availability begins. Further, some distance must be traveled along the lane before the turn can be completed. The to_offset and distance fields provide the information necessary to calculate the destination point from a turn location between start and end. To_offset gives the location along to_lane that is longitudinally equivalent to start. In other words, to_offset would represent the destination point of a turn taken at start if the distance requirement of the turn was zero. Distance represents the distance requirement of the turn was starcent final destination point along to_lane can be calculated using the following formula:

Location = to_offset + (turn location) - start + distance.

As with the point turn table, proper sorting of the linear turn table must be maintained for efficient access. Clearly the primary key must again be lane_id, so that the set of turns for a lane can be quickly found. Further sorting criteria are less obvious. A common need in an application using this data model would be to find the set of turns available at a given point along the lane. If the table is sorted with start as the secondary key, all turns with a start value higher than the current position can be quickly eliminated. However, since linear turns can, and often will, extend the entire length of a lane, each turn with start less than or equal to the current position would need to be examined in turn.

6.3 Impedance points

The previous discussions ignore a fundamental element of transportation networks, impedance associated at a point where no turn is made. This impedance could represent a stop sign, slowdown due to merging traffic, or other legal or physical restriction. This type of impedance is handled in this data model by the use of impedance points. Because impedance points share two of the key attributes of point turns, namely a single location and an associated impedance, it is a simple matter to store them in the point turn table. The two attributes they do not share, to_lane and to_position, can be ignored or made equal to lane_id and position, respectively. Either method is sufficient to distinguish an Impedance point from a turn.

The fundamental difference between impedance points and point turns is the way that they are applied. A point turn represents an option available at that location on the lane, generally with an associated impedance, while an impedance point is automatically applied when a particular location is reached, if no turn option is taken at that point. Impedance points can also be used to represent the end points of lanes, as a point of infinite impedance. While lane endings are stored in the lane table, it may prove desirable to include this information in the turn tables as well, for some applications.

7. ITS Functions

Any research into the development of an effective digital map database for transportation purposes must accept the responsibility to provide for the integration of ITS methods and functionality into the database. It is, in fact, the inability of current data models to efficiently support this flexibility that has initiated the research at hand. According to NCGIA (1994) it is well recognized that "most of the anticipated functions of ITS rely on the existence of an accurate, dependable map database, with sufficient information on network connectivity and driving conditions to allow solution of such problems as determination of the shortest path between a given origin and destination." The map database and ITS functions will be integrated, and the ways in which to do so most effectively must be considered during the development process.

vehicle routing. do interface with the navigable map database are primarily associated with unconcerned with the ability to navigate across it. These include secondary with specific static positions on the map database but will still be relatively navigation is not a concern. Other functions will be associated more closely with the digital map database. Some will be entirely independent of the digital payment stations, and various administrative functions. Those functions that information sources regarding traveler services, safety checkpoints, electronic systems will receive and transmit location information about vehicles. devices do not interact with the navigable map database. At most these example, several types of collision avoidance systems and in-vehicle safety infrastructure that will necessarily accompany a fully functional ITS. map database, but will rely on the communications and information transfer given as potential ITS applications vary in the extent to which they will interact Program. As discussed in the NCGIA Final Report, the individual systems needs must be satisfied by the underlying digital map database. In an effort to determining which functions will compose a fully functional ITS, and what specializations and countless applications. Each of these deserves a voice in has produced a Program Plan for the Intelligent Vehicle Highway Systems record these diverse needs the U.S. Department of Transportation (USDOT) Transportation planning is, however, a broad based discipline with many

7.1 Vehicle Routing

The ITS must be able to provide an initial trip route (based on destination information provided by the user along with historical travel time data and dynamic incident information), update that route as conditions change, guide the user across the route, and inform the user of any pertinent information. Normally, shortest path algorithms developed in mathematical graph theory are used in routing applications on planar networks. Traditional planar networks correspond very well to mathematical graphs, so the use of graph theory algorithms is straightforward. A mathematical graph is an object consisting of a set of elements called vertices and a set of pairs of vertices called edges (McHugh 1990). Relating this to a planar transportation network, vertices correspond to nodes and edges correspond to links. With the non-planar model presented here, existing algorithms cannot be so directly applied.

Graph theory shortest path algorithms such as Dijkstra's (Dijkstra 1959) rely on the structure of a graph, with each edge connected to other edges only at its endpoints. This is not the case with the lane based model, where turns are possible at many points along a lane. Further, as discussed in the previous sections, lanes are frequently connected by linear lane change segments, rather than simple intersections. Because of this, routing on the lane based model requires either the development of a new shortest path algorithm or a method of fitting a mathematical graph to the lane based model so that existing algorithms can be used. The most practical approach appears to be the latter.

O(V'), where V is the number of vertices (McHugh 1990). It is easy to see that edges. The time required to complete Dijkstra's algorithm, for instance, is would need to be represented, for routing purposes, by a large number of than the distance required to change lanes. For a typical highway, each lane segment could be represented by 528 10 foot edges. To avoid artificially made to adjacent lanes at any vertex along the series. For example, a 1 mile segment represented by a series of these edges so that a change can be solution would be to define a minimum edge length, with a continuous any point along a segment, explicit representation of the segment in a graph this would quickly become too large for real time routing. imposing turn restrictions, this edge length would need to be significantly less dealing with continuous lane change segments. Because a turn can occur at would require an infinite number of vertices, clearly an impossibility. One The chief difficulty in fitting a mathematical graph to the lane based model is

congestion, construction, accidents) change drastically. be avoided by allowing lane changes at points where lane conditions (i.e. points the road would be impassible without multiple lane changes. This could blockages. For instance, on a two lane road, if each lane is blocked at severa assumption could be problematic in situations with large numbers of lane linear turn possibility to a turn at a point. It should be noted that only connection between the lanes. In effect, this dynamically reduces the placed at the first possible position along the lane, with that vertex being the as possible if it is made at all. Using this assumption, a vertex would be An alternative to this would be to assume that a lane change is made as soon

allows a higher level of detail than previously achieved, and permits additional of the network. The inclusion of lanes as the primary geographic element substantial reduction in the number of features to be maintained in the road condition information to be utilized, such as the closure of specific lanes adopted here in order to more realistically portray human perceptions of real centerline based, transportation network. A fully non-planar representation is due to accidents or construction. to which this improvement is realized is a function of the size and connectivity database, and eliminates redundancies among feature attributes. The extent world transportation networks. It is clear that non-planar networks allow a This paper represents a significant departure from the traditional planar

integration of GPS spatial referencing, simulated real-time traffic conditions arterial, and highway traffic conditions. Further research will include the and in-vehicle navigation tools to provide a dynamic routing system number of urban and suburban road configurations which represent local, used to reference lane features for a test area. The test area includes a At this time a prototype non-planar network has been developed and is being

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